

## Viewing

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- map 3d world points to 2d image plane positions
  - two stages
- viewing transform
  - map world coordinates to camera coordinates
  - change of coordinate system
- projection
  - map camera coordinates to image plane coordinates
  - orthographic or perspective

## Viewing Transform

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- any affine transform
- useful to define one for our viewer model
  - defined by origin, forward, up
- computed by
  - orthonormalize frame from the vectors
  - construct a matrix for a change of coord. syst.
  - seen in previous lecture

## Projection

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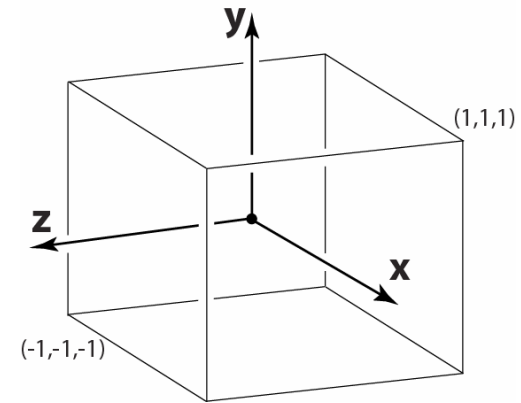
- in general, function that transforms points from  $m$ -space to  $n$ -space where  $m > n$
- in graphics, maps 3d points to 2d image coordinates

## Canonical View Volume

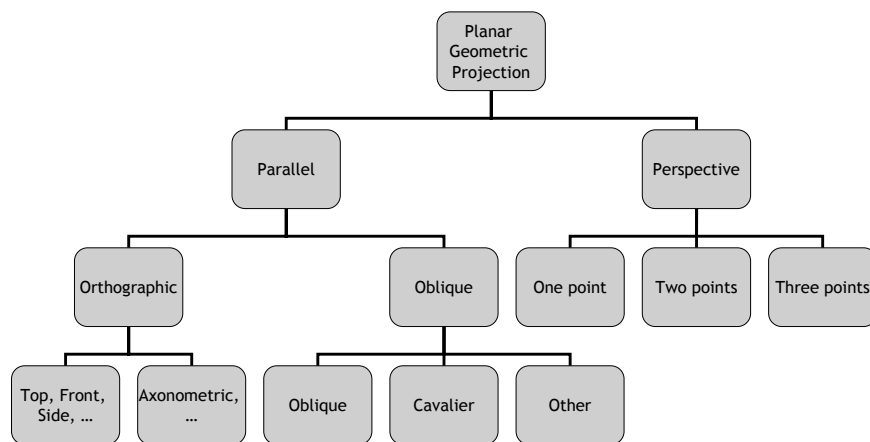
- the result of a projection
  - everything out of it will not be rendered
- $(x,y)$  are image plane coordinates in  $[-1,1] \times [-1,1]$
- keep around the  $z$  normalized in  $[-1,1]$ 
  - define a near and far distance
    - everything on the *near plane* has  $z=1$
    - everything on the *far plane* has  $z=-1$
    - inverted  $z$ !
  - will become useful later on

## Canonical View Volume

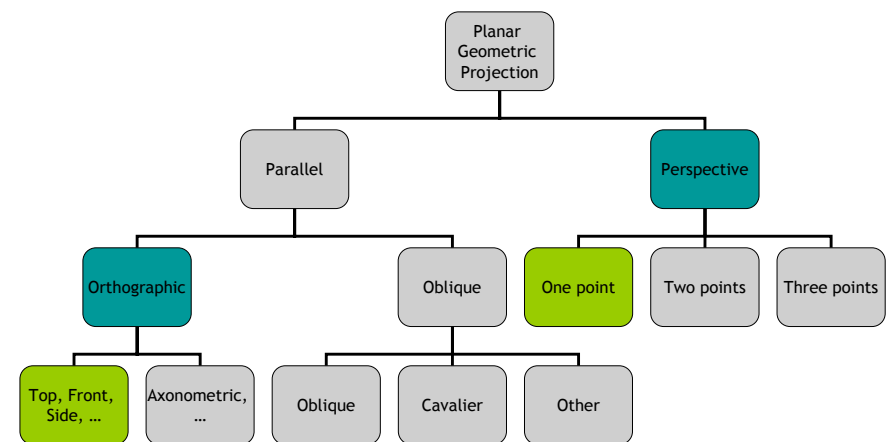
- why introducing near/far clipping planes?
  - mostly to reduce  $z$  range, motivated later



## Taxonomy of projections



## Taxonomy of projections

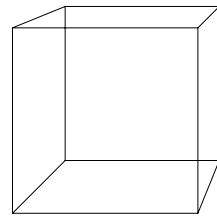
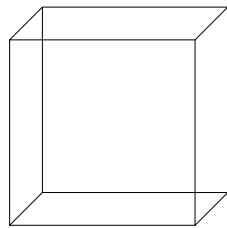
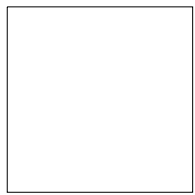


## Taxonomy of projections

Orthographic

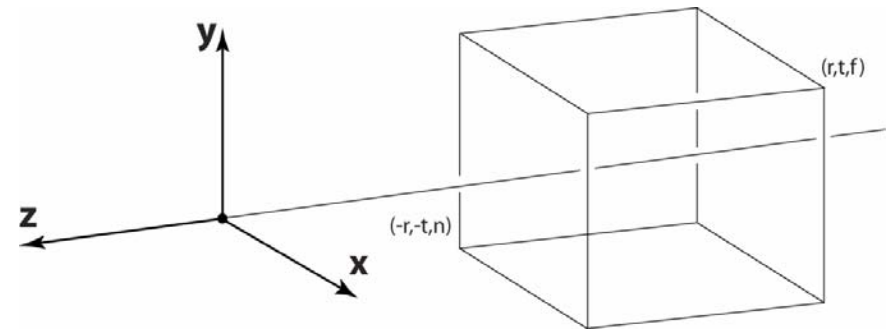
Oblique

Perspective



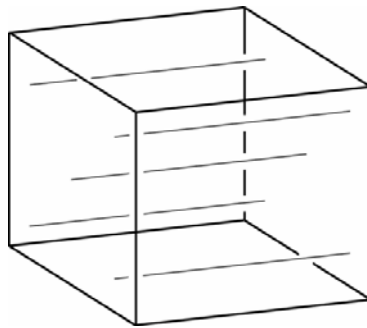
## Orthographic Projection

- box view volume



## Orthographic Projection

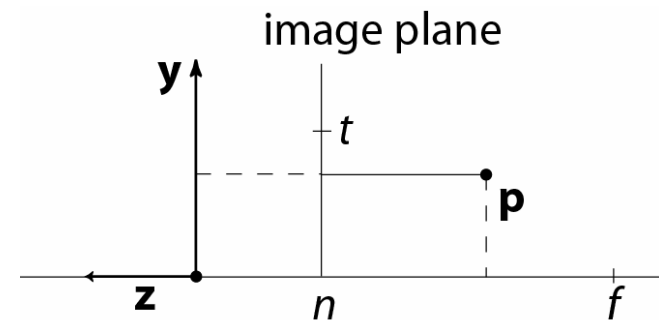
- viewing rays are parallel



## Orthographic Projection

- centered around z axis

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} x/r \\ y/t \\ (2z - n - f)/(n - f) \end{bmatrix}$$



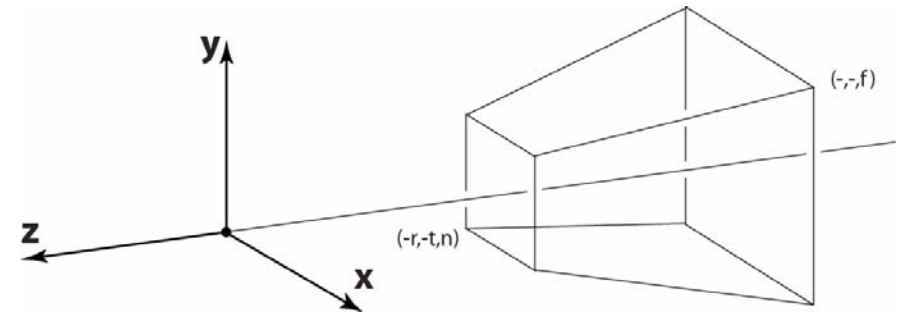
## Orthographic Projection

- write in matrix form

$$\begin{bmatrix} 1/r & 0 & 0 & 0 \\ 0 & 1/t & 0 & 0 \\ 0 & 0 & 2/(n-f) & -(n+f)/(n-f) \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

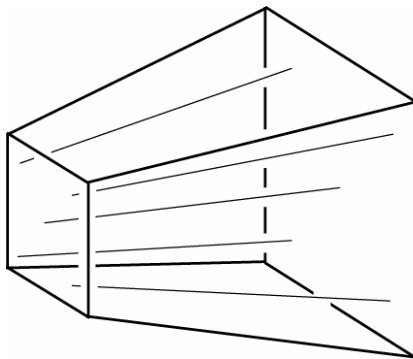
## Perspective Projection

- truncated pyramid view volume



## Perspective Projection

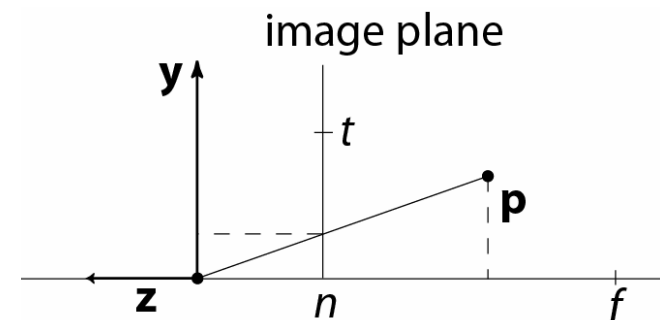
- viewing rays converge to a point



## Perspective Projection

- centered around z axis

$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} (nx)/(rz) \\ (ny)/(tz) \\ \dots \end{bmatrix}$$



## Perspective Projection

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- write it in matrix form
  - use homogeneous coordinates, since  $w \neq 1$ !

$$\begin{bmatrix} n/r & 0 & 0 & 0 \\ 0 & n/t & 0 & 0 \\ 0 & 0 & (f+n)/(n-f) & -2fn/(n-f) \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

## Projection Properties

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- orthographic projection is affine
- perspective projection is not
  - *does not map origin to origin*
  - *maps lines to lines*
  - *parallel lines do not remain parallel*
  - *length ratios are not preserved*
  - *closed under composition*

## More on projections

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- the given matrices are simplified cases
- should be able to define more general cases
  - non-centered windows
  - non-square windows
- can find derivation in the Shirley's book
  - but it is a simple extension of these
- note that systems have different conventions
  - pay attention at their definition
  - sometimes names are the same

## General Orthographic Projection

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$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & \frac{l+r}{l-r} \\ 0 & \frac{2}{t-b} & 0 & \frac{b+t}{b-t} \\ 0 & 0 & \frac{2}{n-f} & \frac{n+f}{n-f} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

## General Perspective Projection

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$$\begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{l+r}{l-r} & 0 \\ 0 & \frac{2n}{t-b} & \frac{b+t}{b-t} & 0 \\ 0 & 0 & \frac{f+n}{n-f} & \frac{2fn}{f-n} \\ 0 & 0 & 1 & 0 \end{bmatrix}$$