

distribution ray tracing

distribution ray tracing

use many rays to compute average values over pixel areas, time, area lights, reflected directions, ...

antialiasing origin

- compute average color subtended by a pixel

pixel center $C = \text{raytrace}(\mathbf{E}, \mathbf{Q} - \mathbf{E})$

pixel average $C = \frac{1}{A_P} \cdot \int_{\mathbf{Q} \in P} \text{raytrace}(\mathbf{E}, \mathbf{Q} - \mathbf{E}) \cdot dA_{\mathbf{Q}}$

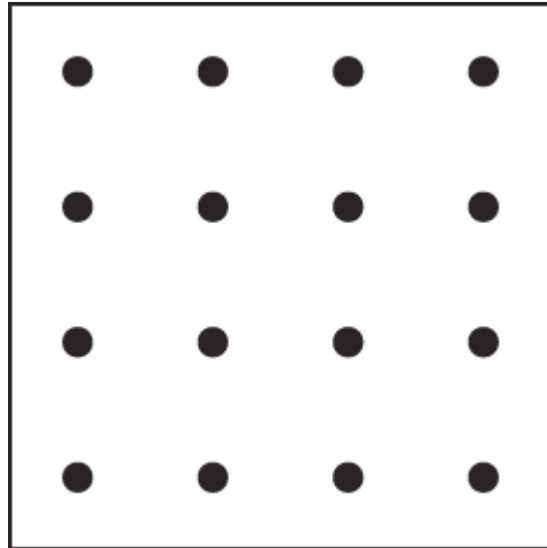
\mathbf{E} : camera origin

\mathbf{Q} : point on image plane

P : pixel of area A_P

antialiasing by deterministic integration

- subdivide the pixel in squares
- cast rays through squares centers
- average result



[Shirley]

deterministic antialiasing pseudocode

- antialiasing pixel (i, j)

$c = 0$

for $sx = 0$ to ns

 for $sy = 0$ to ns

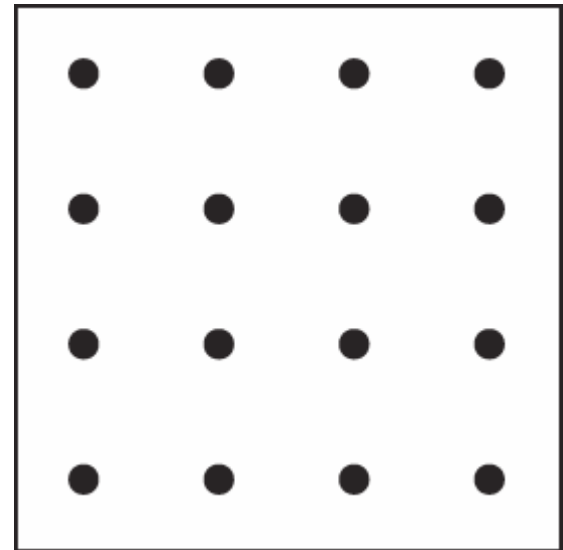
$u = (i + (sx+0.5)/ns) / \text{width}$

$v = (j + (sj+0.5)/ns) / \text{height}$

$Q = \text{imagePlanePoint}(u, v)$

$c += \text{raytrace}(E, Q-E)$

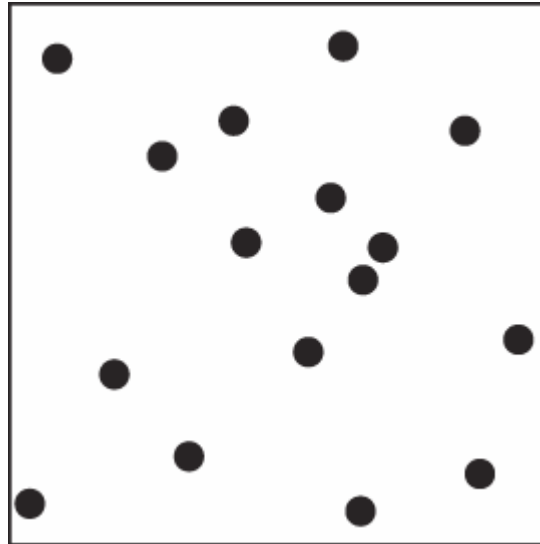
$c /= ns^2$



[Shirley]

antialiasing by Monte Carlo estimation

- pick random points in pixel area
- cast rays through them
- average result



[Shirley]

Monte Carlo antialiasing pseudocode

- antialiasing pixel (i, j)

$c = 0$

for $s = 0$ to ns^2

$(rx, ry) = \text{random2d}();$

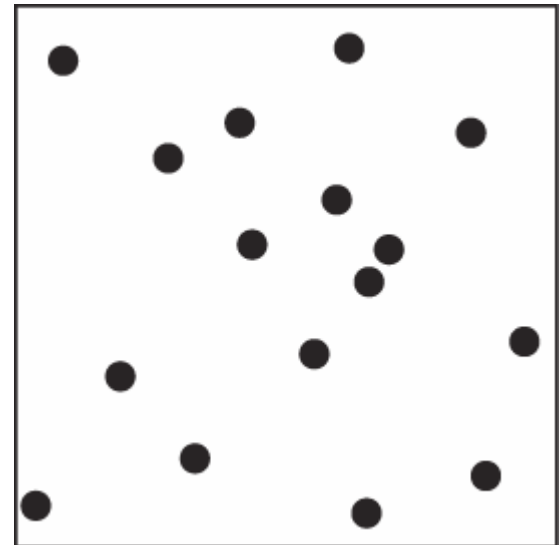
$u = (i + rx) / \text{width}$

$v = (j + ry) / \text{height}$

$Q = \text{imagePoint}(u, v)$

$c += \text{raytrace}(E, Q-E)$

$c /= ns^2$



[Shirley]

Monte Carlo antialiasing pseudocode

- antialiasing pixel (i, j)

$c = 0$

for $sx = 0$ to ns

 for $sy = 0$ to ns

$(rx, ry) = \text{random2d}();$

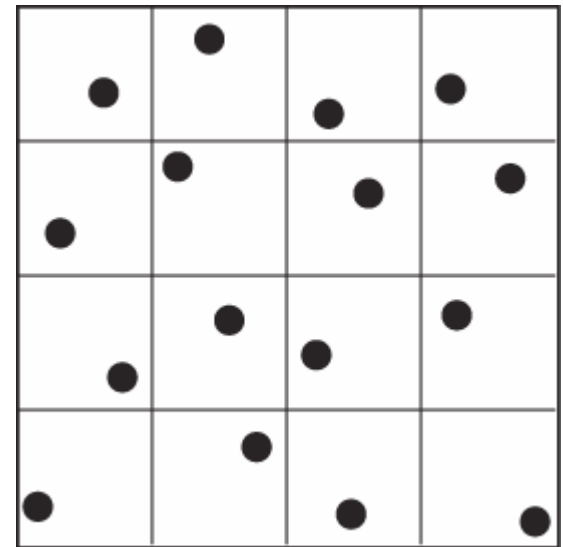
$u = (i + (sx+rx)/ns) / \text{width}$

$v = (j + (sy+ry)/ns) / \text{height}$

$Q = \text{imagePoint}(u, v)$

$c += \text{raytrace}(E, Q-E)$

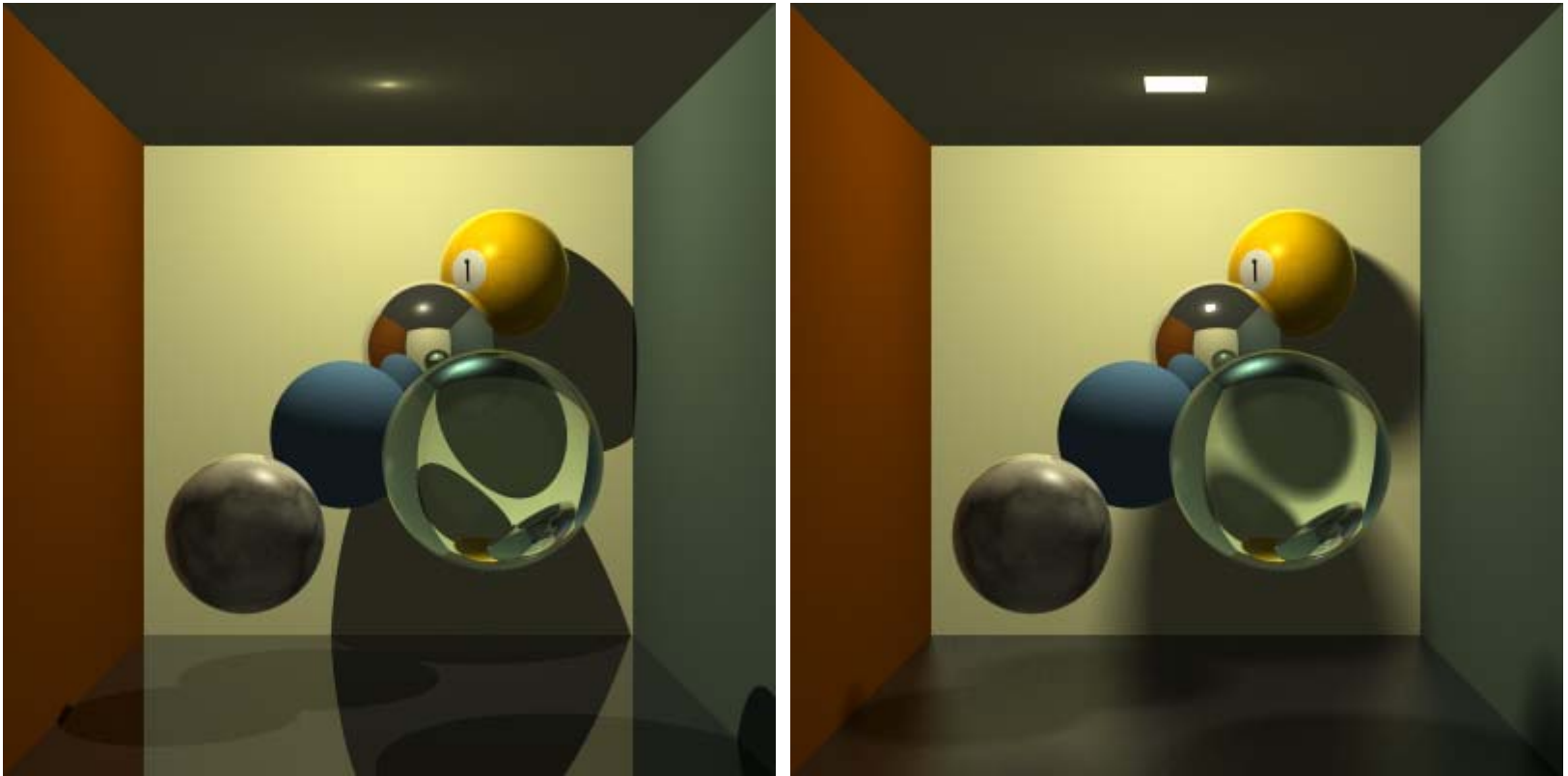
$c /= ns^2$



[Shirley]

raytraced images are too “clean”

- soft shadows come from area light
 - raytracing only supports point lights



[Jason Waltman / jasonwaltman.com]

raytraced images are too “clean”

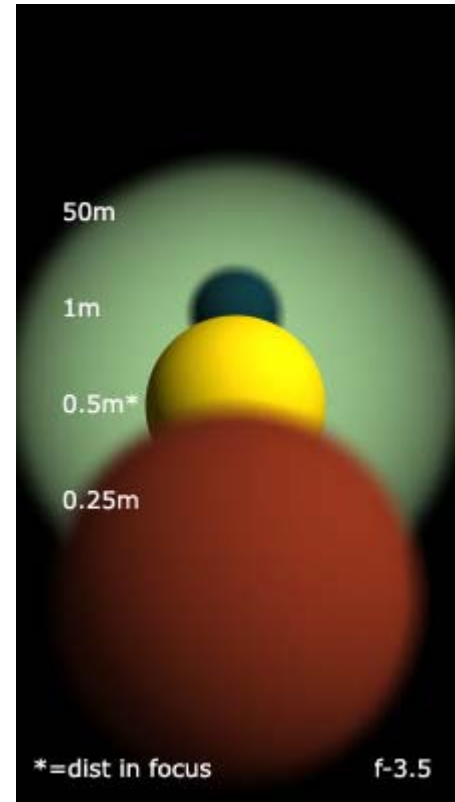
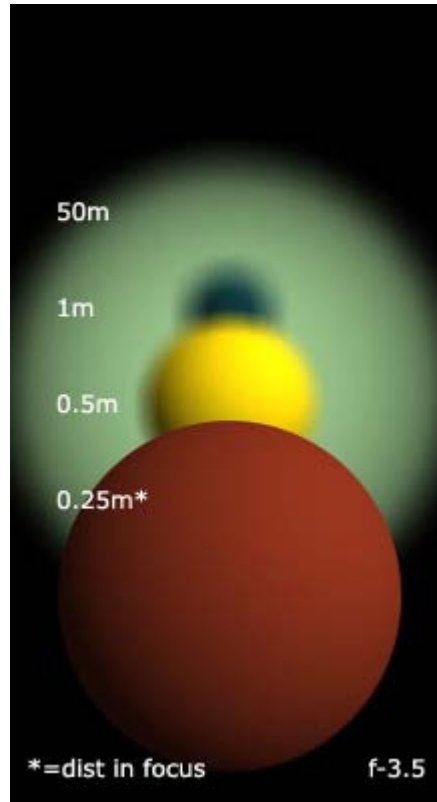
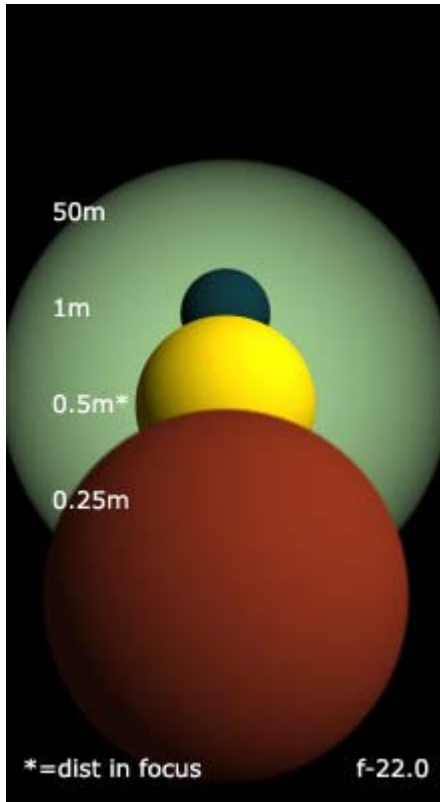
- blurry reflections come from rough materials
 - raytracing only supports perfectly sharp mirrors



[Jensen]

raytraced images are too “clean”

- depth of field come from lens system
 - raytracing only supports pinhole camera



[Jason Waltman / jasonwaltman.com]

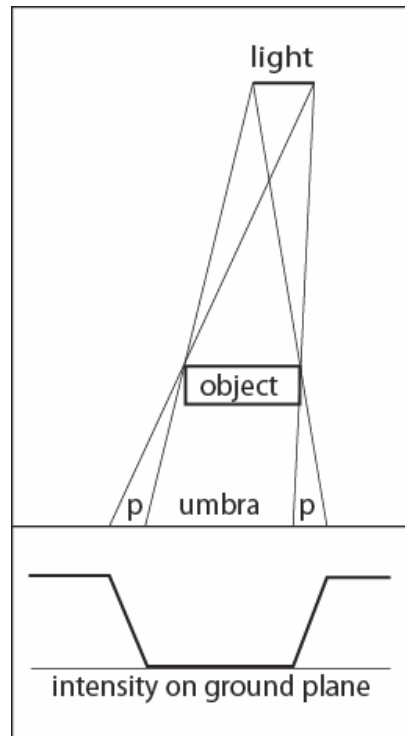
raytracer images are too “clean”

- motion blur come from shutter speed
 - raytracing only support infinitely fast shutter speed



soft shadows origin

- area lights create penumbras
 - light is only partially visible from a given point
 - want to compute how much light hits the point



[Shirley]

approximate soft shadows principle

point light $C = C_l \cdot V(\mathbf{P}, \mathbf{S}) \cdot \text{shading}(\mathbf{P}, \mathbf{S})$

area light $C = \frac{C_l}{A_L} \cdot \int_{\mathbf{S} \in L} V(\mathbf{P}, \mathbf{S}) \cdot \text{shading}(\mathbf{P}, \mathbf{S}) \cdot dA_S$

\mathbf{P} : point on the surface

\mathbf{S} : point on the light

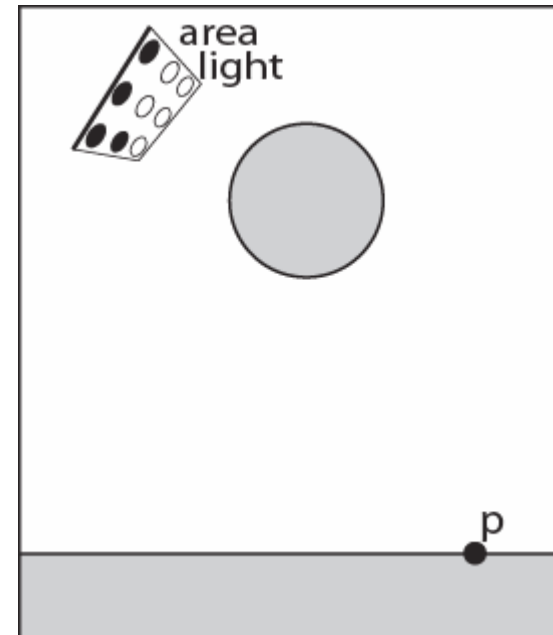
V : visibility function (0 or 1)

L : light of area A_L

C_l : total light intensity

soft shadows by deterministic integration

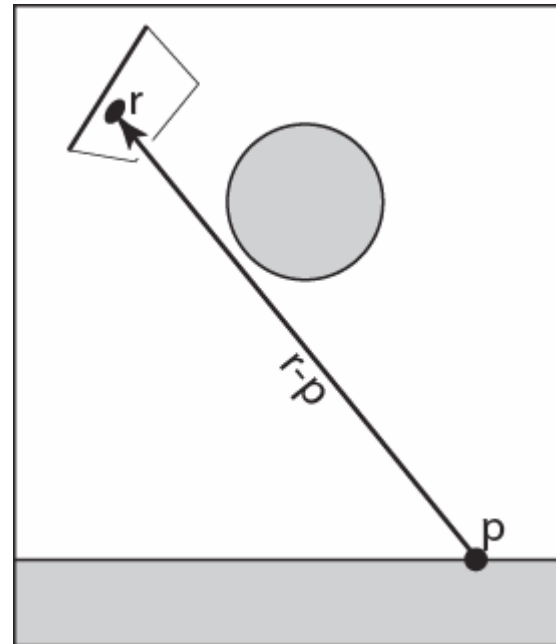
- approximate area light as a set of point lights
 - equivalent to quadrature rule
- for each point, compute shadows and lighting
- average results



[Shirley]

soft shadows by Monte Carlo estimation

- use Monte Carlo integration
- pick random points on the light
 - easy for quad lights, hard (but possible) for others
- compute shadows and lighting
- average results



[Shirley]

soft shadows by Monte Carlo estimation

$$\mathbf{S}_i = \mathbf{S}_c + (0.5 - r_{i,1})l\mathbf{u} + (0.5 - r_{i,2})l\mathbf{v}$$

for quads

$$\langle C \rangle = \frac{C_l}{N} \cdot \sum_i^N V(\mathbf{P}, \mathbf{S}_i) \cdot \text{shading}(\mathbf{P}, \mathbf{S}_i)$$

\mathbf{S}_c : light source center

\mathbf{u}, \mathbf{v} : light source tangent vectors

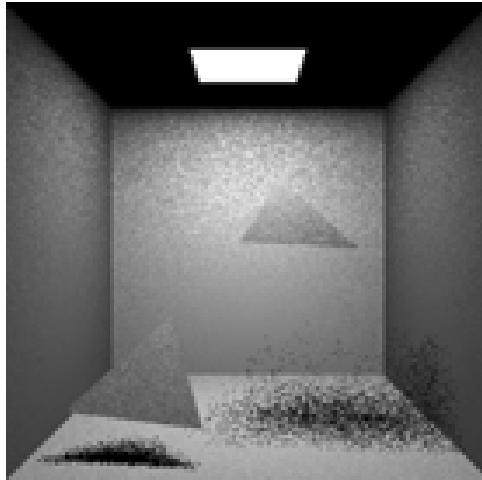
l : light source size

\mathbf{r}_i : uniformly sampled random 2d vector in $[0, 1]^2$

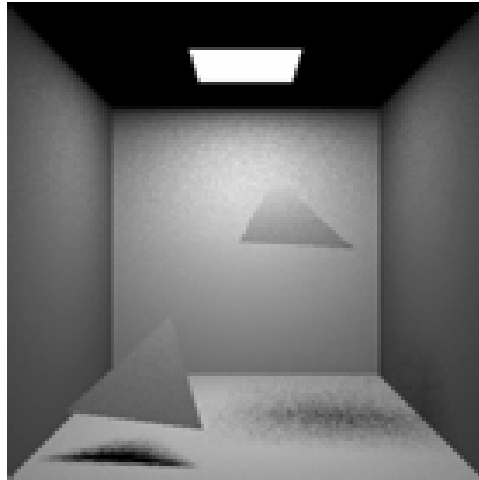
N : total number of samples

how many samples?

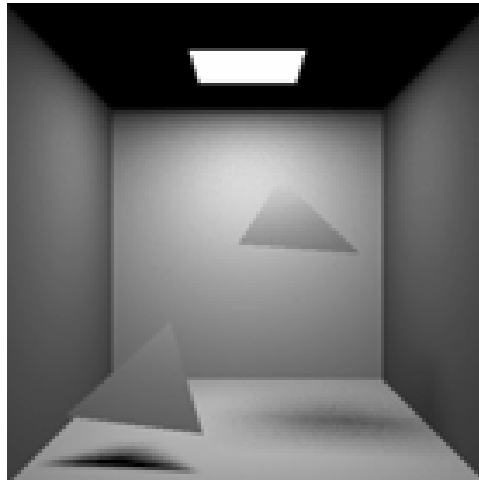
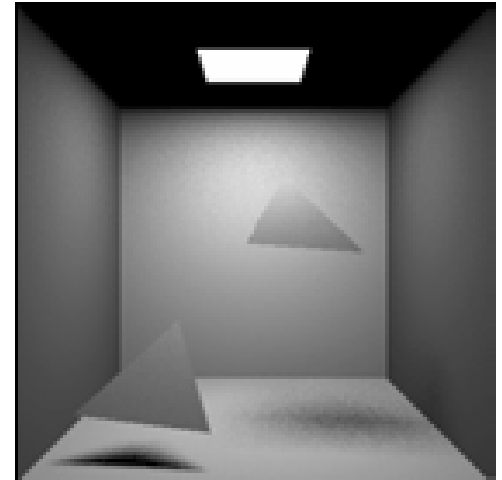
1 sample



9 samples



36 samples

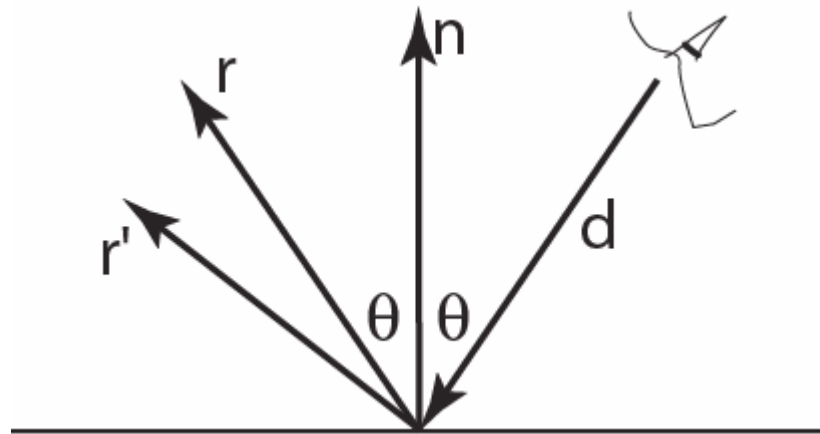


100 samples

[Bala]

blurry reflections origin

- real materials often have blurred reflections
 - light is scattered around a set of directions
 - want to compute how much light reaches the surface along these directions



[Shirley]

approximate blurry reflections principle

mirror refl. $C = k_r \cdot \text{raytrace}(\mathbf{P}, \mathbf{R})$

blurry refl. $C = \frac{k_r}{A_\Omega} \cdot \int_{\mathbf{R} \in \Omega} \text{raytrace}(\mathbf{P}, \mathbf{R}) \cdot dA_{\mathbf{R}}$

P : point on the surface

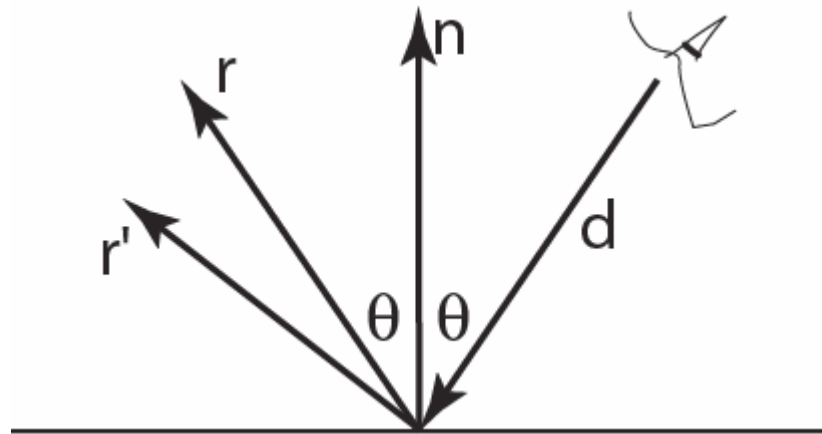
R : reflected direction

Ω : solid angle where object is reflecting

k_r : reflection coefficient

blurred reflection by Monte Carlo est.

- compute reflected direction \mathbf{R}
- pick random direction \mathbf{R}' around \mathbf{R}
- compute reflected color along \mathbf{R}'
- average results



[Shirley]

blurred reflection by Monte Carlo est.

$$\mathbf{R}_i = [\mathbf{R} + (0.5 - r_{i,1})l\mathbf{u} + (0.5 - r_{i,2})l\mathbf{v}] / |\mathbf{R}_i|$$

for quads

$$\langle C \rangle = \frac{k_r}{N} \cdot \sum_i^N \text{raytrace}(\mathbf{P}, \mathbf{R}_i)$$

\mathbf{R} : reflected direction

\mathbf{u}, \mathbf{v} : vectors orthogonal to \mathbf{R}

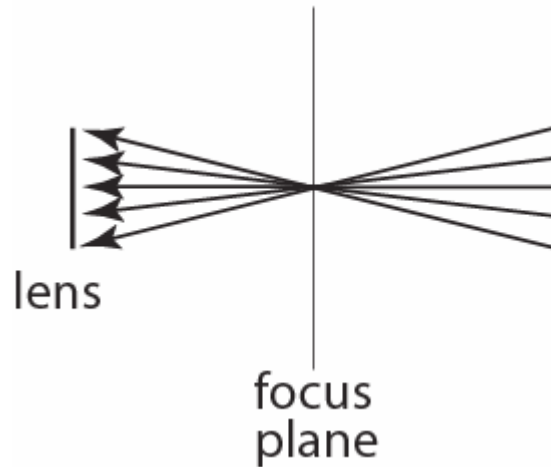
l : blur size

\mathbf{r}_i : uniformly sampled random 2d vector in $[0, 1]^2$

N : total number of samples

depth-of-field origin

- images in eyes and cameras are formed by lenses
 - not all rays converge to a point
 - so only some object appear sharp (in focus)
 - while all other objects do not (out of focus)



[Shirley]

approximate depth-of-field principle

pinhole $C = \frac{1}{A_P} \int_{\mathbf{Q} \in A_P} \text{raytrace}(\mathbf{E}, \mathbf{Q} - \mathbf{E}) dA_Q$

dof $C = \frac{1}{A_P A_L} \cdot \int_{\mathbf{Q} \in P} \int_{\mathbf{F} \in L} \text{raytrace}(\mathbf{F}, \mathbf{Q} - \mathbf{F}) \cdot dA_F \cdot dA_Q$

\mathbf{E} : camera origin

\mathbf{Q} : point on image plane

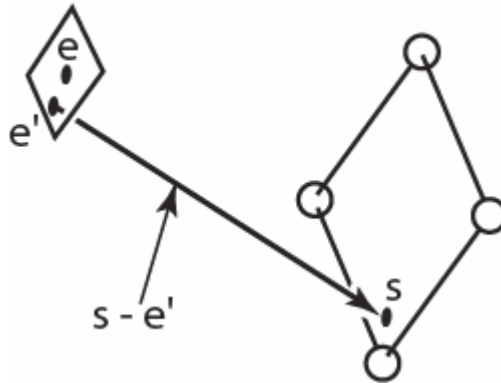
\mathbf{F} : point on "lens" plane around \mathbf{E}

P : pixel of area A_P

L : lens of area A_L

depth-of-field by Monte Carlo estimation

- pick random points on film and image plane
- compute color from aperture point toward image one
- average results



[Shirley]

depth-of-field by Monte Carlo estimation

$$\mathbf{F}_i = \mathbf{E} + (0.5 - s_{i,1})l_a \mathbf{u} + (0.5 - s_{i,2})l_a \mathbf{v}$$

for quads $\mathbf{Q}_i = \mathbf{E} + (x + 0.5 - r_{i,1})l_p \mathbf{u} + (y + 0.5 - r_{i,2})l_p \mathbf{v} - n\mathbf{z}$

$$\langle C \rangle = \frac{1}{N} \cdot \sum_i^N \text{raytrace}(\mathbf{F}_i, \mathbf{Q}_i - \mathbf{F}_i)$$

\mathbf{u}, \mathbf{v} : vectors parallel to image plane

l_P, l_L : pixel/aperture size

n : distance to image plane

$\mathbf{r}_i, \mathbf{s}_i$: uniformly sampled random 2d vectors in $[0, 1]^2$

N : total number of samples

motion blur origin

- takes time for images to form on camera/eye
 - during that time the camera/eye is open
 - sensors take the “average” of what’s happening
 - but objects move around in that time

approximate motion blur principle

no blur $C(t) = \text{raytrace}(\mathbf{E}, \mathbf{I}, S_t)$

blurry refl. $C(t, \Delta t) = \frac{1}{\Delta t} \cdot \int_{s \in [t, t + \Delta t]} \text{raytrace}(\mathbf{E}, \mathbf{I}, S_s) \cdot dl_s$

\mathbf{E} : any ray origin

\mathbf{I} : any ray direction

S_t : scene at time t

t : time when shutter opens

Δt : time that shutter stays open

$\Delta t = t_{k+1} - t_k$: for animation, time between frames

motion blur by Monte Carlo estimation

- for any ray (camera, shadow, reflection), pick random time in the shutter interval
- update object transformations for picked time
- compute intersection
- average results

motion blur by Monte Carlo estimation

for aliased camera rays

$$\langle C \rangle = \frac{1}{N} \cdot \sum_i^N \text{raytrace}(\mathbf{E}, \mathbf{Q} - \mathbf{E}, S_{t_i})$$

\mathbf{E} : camera origin

\mathbf{Q} : point on image plane

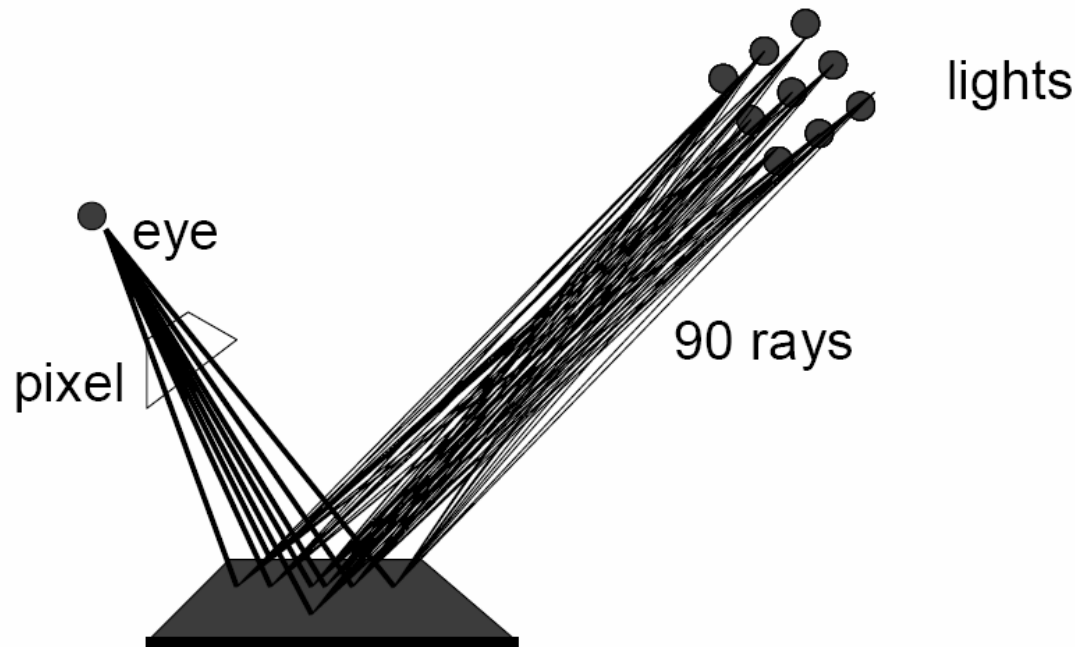
t_i : uniformly sampled random variable in $[0, 1]$

N : total number of samples

combining estimations

- e.g. compute soft shadows and antialias the pixel

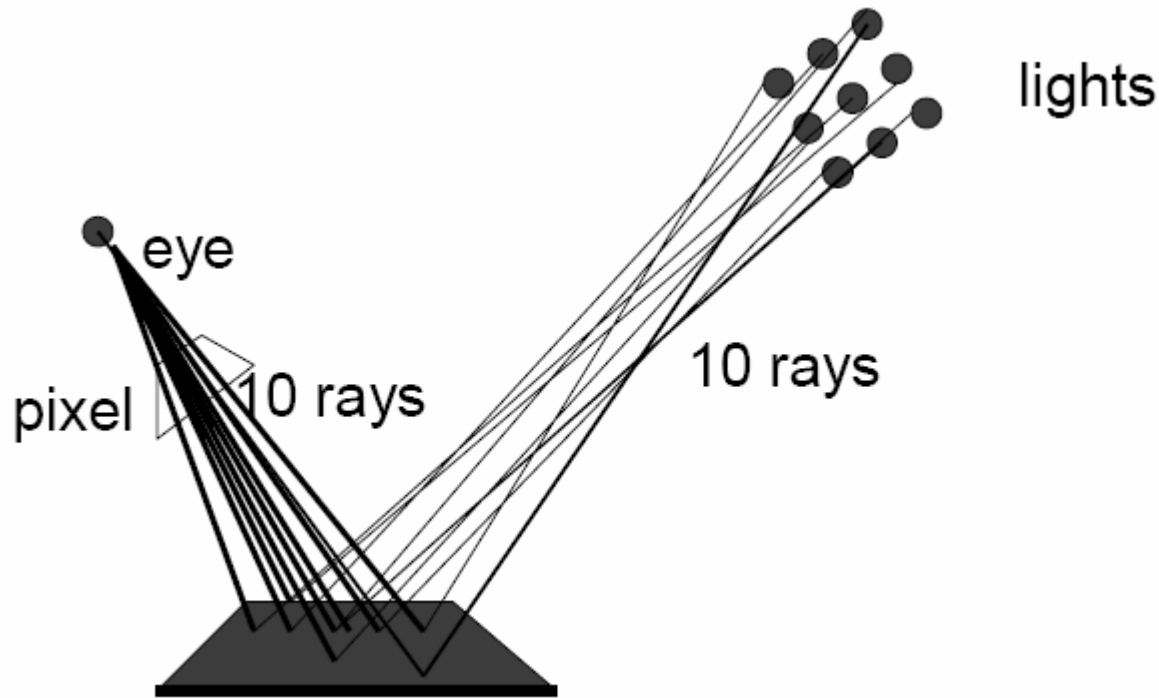
$$C = \frac{C_l}{A_P A_L} \cdot \int_{\mathbf{Q} \in A_P} \int_{\mathbf{S} \in A_L} V(\mathbf{P}(\mathbf{Q}), \mathbf{S}) \cdot \text{shading}(\mathbf{P}(\mathbf{Q}), \mathbf{S}) \cdot dA_S \cdot dA_Q$$



[Bala]

combining estimations: path tracing

- idea: *randomize the whole path*
 - compute all the integrals at once!



[Bala]